

FIRE MATHEMATICS CLASSES

Add :- Deepak Store Gali, Near of Bio-Centre

By :- P.R. Raman Sir

Mob :- 9097873579

The Selection of Good Question 2025

► INVERSE TRIGONOMETRIC FUNCTION

1. Find the Principle value of

(i) $\sin^{-1} \left(\frac{\sqrt{3}}{2} \right)$

(ii) $\cos^{-1} \left(\frac{-1}{2} \right)$

(iii) $\tan^{-1}(-1)$

2. Prove that

(a) $\tan^{-1}x + \cot^{-1}x = \frac{\pi}{2}$

(e) $\sin^{-1} \frac{8}{17} + \sin^{-1} \frac{3}{5} = \tan^{-1} \frac{77}{36}$

(b) $\cos\{\sec^{-1}x + \operatorname{cosec}^{-1}x\} = 0$ (f) $2 \sin^{-1} \frac{3}{5} = \tan^{-1} \frac{24}{7}$

(c) $\sin\left\{\sin^{-1} \frac{1}{2} + \cos^{-1} \frac{1}{2}\right\} = 1$ (g) $2 \tan^{-1} \frac{1}{2} + \tan^{-1} \frac{1}{7} = \tan^{-1} \frac{31}{17}$

(d) $\tan^{-1} \frac{1}{5} + \tan^{-1} \frac{1}{7} + \tan^{-1} \frac{1}{3} + \tan^{-1} \frac{1}{8} = \frac{\pi}{4}$

3. $\sin^{-1} \left\{ \sin \frac{2\pi}{3} \right\} = ?$

4. $\cos^{-1} \left\{ \cos \frac{7\pi}{6} \right\} = ?$

5. $\tan^{-1}\sqrt{3} - \sec^{-1}(-2) = ?$

6. $\tan^{-1} \frac{1}{2} + \tan^{-1} \frac{2}{11} = \tan^{-1} p$ find p.

7. $2 \tan^{-1} \frac{1}{3} + \tan^{-1} \frac{1}{7} = \frac{\pi}{4}$

8. $4 (\cot^{-1} 3 + \operatorname{cosec}^{-1} \sqrt{5}) = \pi$

9. $\frac{9\pi}{8} - \frac{9}{4} \sin^{-1} \frac{1}{3} = \frac{9}{4} \sin^{-1} \frac{2\sqrt{2}}{3}$

10. $\cot^{-1} \left\{ \tan \frac{\pi}{4} \right\} = ?$

11. $\cot^{-1} \left\{ \frac{\sqrt{1+\sin x} + \sqrt{1-\sin x}}{\sqrt{1+\sin x} - \sqrt{1-\sin x}} \right\} = \frac{x}{2}$

❖ Solve or, find the value of x.

12. $\tan^{-1} 2x + \tan^{-1} 3x = \frac{\pi}{4}$

15. $\tan \left\{ \sin^{-1} \frac{3}{5} + \cot^{-1} \frac{3}{2} \right\}$

13. $2 \tan^{-1}(\cos x) = \tan^{-1}(2 \operatorname{cosec} x)$

16. $\tan^{-1} \left[2 \cos \left(2 \sin^{-1} \frac{1}{2} \right) \right]$

14. $\tan^{-1} \left\{ \frac{\cos x - \sin x}{\cos x + \sin x} \right\}$

17. $\sin \left\{ \frac{\pi}{3} - \sin^{-1} \left(\frac{-1}{2} \right) \right\}$

18. $\sin^{-1}(1-x) - 2 \sin^{-1}x = \frac{\pi}{2}$ then the value of x

► DIFFERENTIATION ** 2ND DELIVATIVE

1. $y = \log x$

2. $y = e^x \cdot \sin x$

3. $y = (\tan^{-1} x)^2$

4. $y = \log(\log x)$
5. prove that $y = 500 e^{7x} + 600 e^{-7x} \frac{d_2y}{dx^2} = 49 y$
6. If $e^y(x+1)$ then prove that $\left(\frac{d_2y}{dx^2} = \frac{dy}{dx}\right)^2$
7. If $y = (\tan^{-1}x)^2$ then prove that $(x^2+1)y_2 + 2x(x^2+1)y_1 = 2$
8. If $y = A \sin x + B \cos x$ then prove that $\frac{d_2y}{dx^2} + y = 0$

► MATRICES

1. If $A = \begin{pmatrix} 2 & 3 \\ 4 & 5 \end{pmatrix}$ then prove that $(A')' = A$
2. $\begin{bmatrix} \cos^2 x & \sin^2 x \\ \sin^2 x & \cos^2 x \end{bmatrix} + \begin{bmatrix} \sin^2 x & \cos^2 x \\ \cos^2 x & \sin^2 x \end{bmatrix} = ?$
3. $A = \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}$ find adj. (A)
4. $A = \begin{bmatrix} 3 & 6 \\ 5 & -4 \end{bmatrix}, B = \begin{bmatrix} 7 & 8 \\ 5 & 6 \end{bmatrix}$ find $2A + 3B$
5. If $A = \begin{bmatrix} 3 & 4 \\ 2 & 3 \end{bmatrix}$ find $A + A'$
6. If $A = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$ find A^2
7. If $A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$ find A^2
8. If $\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \cdot \begin{bmatrix} 3 & 2 \\ 2 & 5 \end{bmatrix} = \begin{bmatrix} 7 & 12 \\ k & 26 \end{bmatrix}$ find k.
9. $\begin{bmatrix} x^2 & -1 \\ 2 & -3 \end{bmatrix} + \begin{bmatrix} -2x & 3 \\ 4 & 5 \end{bmatrix} = \begin{bmatrix} -1 & 2 \\ 6 & 2 \end{bmatrix}$ find x.
10. If $x+y = \begin{bmatrix} 7 & 0 \\ 2 & 5 \end{bmatrix}$ and $x-y = \begin{bmatrix} 3 & 0 \\ 0 & 3 \end{bmatrix}$ find $x-y$.
11. $A = \begin{bmatrix} a & 0 \\ 1 & 1 \end{bmatrix}, B = \begin{bmatrix} 1 & 0 \\ 5 & 1 \end{bmatrix}$ Where $A^2 = B$ find a.
12. $A = \begin{bmatrix} 2 & 3 \\ 5 & -2 \end{bmatrix}$ find A^{-1}
13. If $A = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$ find A^{-1}
14. If $A = \begin{bmatrix} 1 & 2 & 5 \\ 3 & 2 & 4 \\ 1 & 9 & 7 \end{bmatrix}$ find A^{-1}
15. If $A = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix}$ then verify $A^2 - 4A - 5I = 0$

16. Express sum of symmetric and skew symmetric matrix of $\begin{bmatrix} 3 & -2 & -4 \\ 3 & -2 & -5 \\ -1 & 1 & 2 \end{bmatrix}$
17. Using matrix solve of the eqⁿ $x + y + z = 6$, $2x + y - 3z = -5$, $3x - 2y + z = 2$

► DETERMINANTS

1. $\begin{vmatrix} 2 & 3 & 5 \\ 0 & 4 & 7 \\ 0 & 0 & 5 \end{vmatrix} = ?$

2. $\begin{vmatrix} 1 & 2 \\ 3 & 4 \end{vmatrix} = ?$

3. $\begin{vmatrix} 102 & 18 & 36 \\ 1 & 3 & 4 \\ 17 & 3 & 6 \end{vmatrix} = ?$

4. $\begin{vmatrix} 3 & 1 & 7 \\ 5 & 0 & 2 \\ 2 & 5 & 3 \end{vmatrix} = ?$

5. $\begin{vmatrix} \sin 20^\circ & -\cos 70^\circ \\ \sin 70^\circ & \cos 70^\circ \end{vmatrix}$

6. $\begin{vmatrix} x & 8 \\ 3 & 3 \end{vmatrix} = 0$ find x

7. $\begin{vmatrix} 1-x & 2 \\ 18 & 6 \end{vmatrix} = \begin{vmatrix} 6 & 2 \\ 18 & 6 \end{vmatrix}$ find x

13. If a, b, c are in A.P then $\begin{vmatrix} x+2 & x+3 & x+2a \\ x+3 & x+4 & x+2b \\ x+4 & x+5 & x+2c \end{vmatrix}$ is

Prove that

14. $\begin{vmatrix} x+y & 2x & 2x \\ 2x & x+y & 2x \\ 2x & x & x+y \end{vmatrix} = (5x+y)(4-x)^2$

15. $\begin{vmatrix} a & b & c \\ a^2 & b^2 & c^2 \\ z^3 & b^3 & c^3 \end{vmatrix} = abc(a-b)(b-c)(c-a)$

16. $\begin{vmatrix} 1 & bc & a(b+c) \\ 1 & ca & b(c+a) \\ 1 & ab & c(a+b) \end{vmatrix} = 0$

17. $\begin{vmatrix} \frac{1}{a} & 1 & ac \\ \frac{1}{b} & 1 & ca \\ \frac{1}{c} & 1 & ab \end{vmatrix} = 0$

8. $A = \begin{bmatrix} 3 & 2 & 7 \\ 8 & 9 & 11 \\ 11 & 11 & 18 \end{bmatrix}$ find $|2A|$

9. $\begin{vmatrix} 1 & w & w^2 \\ w & w^2 & 1 \\ w^2 & 1 & w \end{vmatrix} = ?$

10. $\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^3 & b^3 & c^3 \end{vmatrix} = ?$

11. $\begin{vmatrix} 1 & a & a^2 \\ 1 & b & b^2 \\ 1 & c & c^2 \end{vmatrix} = ?$

12. $\begin{vmatrix} x & x^2 & x^3 \\ y & y^2 & y^3 \\ z & z^2 & z^3 \end{vmatrix} = ?$

18. $\begin{vmatrix} 2 & 7 & 65 \\ 3 & 8 & 75 \\ 5 & 9 & 86 \end{vmatrix} = 0$

19. $\begin{vmatrix} 1 & a & b+c \\ 1 & b & c+a \\ 1 & c & a+b \end{vmatrix} = 0$

► | लली POPवाला मुखरा

Find $\frac{dy}{dx}$

1. $y = \sqrt{x + \sqrt{x + \sqrt{x + \sqrt{x + \dots}}}}$ to ∞
2. $y = x^x$
3. $y = (\sin x)^{\cos x} + (\cos x)^{\sin x}$
4. $x^{x^x\dots\infty}$
5. $y = e^{e+e^x+e^{x+\dots} \dots \text{to } \infty}$
6. $y = \sqrt{\sin x + \sqrt{\sin x + \sqrt{\sin x + \dots}}} \dots \text{to } \infty$
7. $y = x^{\sin x} + (\sin x)^{\cos x}$
8. $x^y = y^x \frac{dy}{dx}$
9. $(\cos x)^y = (\cos y)^x$ find $\frac{dy}{dx}$
10. $xy = e^{x-y}$ find $\frac{dy}{dx}$
11. $y = 3e^{2x} + 2e^{3x}$ show that $\frac{d^2y}{dx^2} - 5\frac{dy}{dx} + 6y = 0$
12. $y = \sin [\cos \{\tan(\cot x)\}]$ find $\frac{dy}{dx}$
13. $y = \sqrt{\sin \sqrt{x}}$
14. $y = e^{\tan^{-1}x}$
15. $x^y \cdot y^x = 1$
16. $y = \sin(\cos x)$
17. $x^m \cdot y^n = (x-y)^{m+n}$
18. $y = e^{x^x}$
19. $y = \sin(\cos^{-1}x)$
20. $y = \tan x^0$
21. $y = \tan^{-1} \frac{2x}{1-x^2}$
22. $y = \log \{x^2 \sqrt{x^2 + 1}\}$
23. $y = \cos x \cdot \cos 2x \cdot \cos 3x$
24. $y = \cos \sqrt{x}$
25. $y = \sqrt{\log x + \sqrt{\log x + \sqrt{\log x + \dots}}} \dots \text{to } \infty$
26. $y = e^x + e^{x^2} + e^{x^3} + \dots + e^{x^5}$
27. $x^2 + xy + y^2 = 100$
28. $y + \sin y = \cos x$
29. $x - y = \pi$
30. $y = (\tan^{-1}x)^2$

► | **INDEFINITE**

Find the following in integrals

1. $\int \frac{1}{\sqrt{x}} dx$
2. $\int \cosec 2x dx$
3. $\int e^{ax} dx$
4. $\int (ax^2 + bx + c) dx$
5. $\int x^2 \left(1 - \frac{1}{x^2}\right) dx$
6. $\int \left(\sqrt{x} - \frac{1}{\sqrt{x}}\right)^2 dx$
7. $\int \sqrt{x}(1-x) dx$
8. $\int \sec x (\sec x + \tan x) dx$
9. $\int 0 dx$
10. $\int \left(x^{\frac{3}{2}} + 2e^x - \frac{1}{x}\right) dx$
11. $\int \frac{x^3 - 1}{x^2} dx$
12. $\int \cosec x (\cosec x + \cot x) dx$
13. $\int \frac{1 - \sin x}{\cos^2 x} dx$
14. $\int \frac{2 - 3 \sin x}{\cos^2 x} dx$
15. $\int (3x^2 + 2x + 3)\sqrt{x} dx$
16. $\int \frac{\sec^2 x}{\cosec^2 x} dx$
17. $\int (\sin x + \cos x)^2 dx$
18. $\int \frac{\cosec x}{\cosec x + \cot x} dx$
19. $\int \frac{x^2 + 5x - 4}{x^2} dx$
20. $\int \frac{x^3 - x^2 + x - 1}{x-1} dx$
21. $\int \frac{1}{x+x \log x} dx$
22. $\int \frac{e^{\tan^{-1} x}}{1+x^2} dx$
23. $\int \frac{1}{x(\log x)^m} dx$
24. $\int \cot x \cdot \log \sin x dx$
25. $\int \frac{\cos \sqrt{x}}{\sqrt{x}} dx$
26. $\int \frac{1}{x-\sqrt{x}} dx$
27. $\int \frac{10^{x+10} + 10^x \log 10}{x^{10+10^x}} dx$
28. $\int \frac{1}{\sin^2 x \cdot \cos^2 x} dx$
29. $\int \frac{\sin^2 x - \cos^2 x}{\sin^2 x \cdot \cos^2 x} dx$
30. $\int \frac{1}{\cos^2 x (1-\tan x)^2} dx$
31. $\int \frac{\cos 2x + 2 \sin x}{\cos^2 x} dx$
32. $\int \frac{\sin x}{(1+\cos x)^2} dx$
33. $\int \sin 2x \cdot \cos 3x dx$
34. $\int \tan x dx$
35. $\int \sec x dx$
36. $\int x^2 \cdot e^{x^3} dx$
37. $\int \cos^2 x dx$
38. $\int \sin^3 x dx$
39. $\int \sin^{-1}(\cos x) dx$
40. $\int \frac{1-\cos x}{1+\cos x} dx$
41. $\int \frac{e^x(1+x)}{\cos^2(e^x \cdot x)} dx$
42. $\int e^x \{\tan x + \log \cos x\} dx$
43. $\int \frac{x e^x}{(x+1)^2} dx$
44. $\int \frac{-1}{x^2+a^2} dx$
45. $\int \frac{1}{x^2+a^2} dx$
46. $\int \frac{1}{1+\sin x} dx$
47. $\int \frac{1}{x^2-16} dx$
48. $\int \frac{1}{9-25x^2} dx$
49. $\int \frac{1}{x^2+2x+2} dx$
50. $\int \frac{x}{(x+1)(x+2)} dx$
51. $\int \frac{(3x-1)}{(x-1)(x-2)(x-3)} dx$
52. $\int \frac{\cos x}{(1-\sin x)(2-\sin x)} dx$
53. $\int \frac{\sec^2 x}{\sqrt{\tan^2 x+4}} dx$
54. $\int \sqrt{x^2 + 4x + 6} dx$
55. $\int e^x \{f(x) + f'(x)\} dx$
56. $\int e^x \left\{ \frac{1}{x} - \frac{1}{x^2} \right\} dx$
57. $\int e^x \{ \tan^{-1} x + \frac{1}{1+x^2} \} dx$
58. $\int e^x \{ \sin x + \cos x \} dx$
59. $\int e^x \cdot \sec x \{ 1 + \tan x \} dx$
60. $\int x \cdot e^x dx$
61. $\int x \cdot \log x dx$
62. $\int x \cdot \tan^{-1} x dx$
63. $\int \log x dx$
64. $\int e^x \cdot \sin x dx$
65. $\int e^x \cdot \cos x dx$

► **DEFINITE INTEGRATION**

1. $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin^7 x dx$
2. $\int_0^1 x(x-x)^{99} dx$
3. $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin^2 x dx$
4. $\int_a^b x^5 dx$
5. $\int_0^\pi \frac{x}{1+\sin x} dx$
6. $\int_0^1 \frac{1}{\sqrt{1-x^2}} dx$
7. $\int_0^{\pi/4} (\tan x - x) \tan^2 x dx$
8. $\int_2^4 \frac{1}{x} dx$
9. $\int_0^a \frac{\sqrt{x}}{\sqrt{x} + \sqrt{x-a}} dx$
10. $\int_0^1 x \cdot e^{x^2} dx$
11. $\int_{-\pi/2}^{\pi/2} (x^3 + x \cos x + \tan^5 x + 1) dx$
12. $\int_{-5}^5 |x+2| dx$
13. $\int_2^3 \frac{1}{x \log x} dx$
14. $\int_0^\pi (\sin^2 \frac{x}{2} - \cos^2 \frac{x}{2})$
15. Prove that $\int_0^{\pi/2} \log \sin x dx = \int_0^{\pi/2} \log \cos x dx = -\frac{\pi}{2} \log_2$
16. Prove that $\int_0^{\pi/4} \log(1 + \tan x) dx = \frac{\pi}{8} \log_2$
17. $\int_0^{\pi/2} (2 \log \sin 2x - \log \sin 2x) dx = -\frac{\pi}{2} \log 2 = \frac{x}{2} \log \frac{1}{2}$
18. $\int_0^{\pi/2} \frac{\sqrt{\cos x}}{\sqrt{\sin x} + \sqrt{\cos x}} dx = \frac{\pi}{4}$
19. $\int_0^{\pi/2} \frac{\cos^5 x}{\cos^5 x + \sin^5 x} dx = \frac{\pi}{4}$
20. $\int_0^{\pi/2} \log \cot x dx = 0$
21. $\int_0^{\pi/2} \sin 2x \cdot \log(\tan x) dx = ?$

► **L.P.P.**

1. Minimize $Z = 5x + 7y$ subject $x + y \leq 3, 3x + 8y \leq 35$ and $x, y \geq 0$
2. Maximize $Z = 5x + 3y$ subject $3x + 5y \leq 15, 5x + 2y \geq 10$ and $x \geq 0, y \geq 0$
3. Maximize $Z = 45x + 80y$ Subject $5x + 20y \leq 400, 10x + 15y \leq 400$ and $x \geq 0, y \geq 0$
4. Minimize $Z = 200x + 500y$ subject $x + 2y \geq 0, 3x + 4y \leq 24, x \geq 0, y \geq 0$
5. Maximize $Z = x + 2y$ subject $2x + y \leq 200, x + 2y \geq 100, 2x - y \leq 0, x, y \geq 0$
6. Min & Max $Z = 5x + 10y$ Subject $x + 2y \leq 120, x + y \geq 60, x - 2y \geq 0$ and $x, y \geq 0$
7. Min & Max $Z = 3x + 9y$ subject $x + 3y \leq 60, x + y \geq 100, x \leq y, x, y \geq 0$

► **VECTOR**

1. The modulus of $2\hat{i} - 7\hat{j} + 3\hat{k}$
2. If $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ find (a) $|\vec{a}|$ (b) \hat{a} (c) D.r (d) D.C

3. If $\vec{a} = 2\hat{i} + 3\hat{j} + 4\hat{k}$ and $\vec{b} = \hat{i} + \hat{j} - \hat{k}$ find $\vec{a} + \vec{b}$ and $\vec{a} - \vec{b}$
4. If $\vec{a} = 2\hat{i} - 5\hat{j} + \hat{k}$ and $\vec{b} = 4\hat{i} + 2\hat{j} + \hat{k}$ then $\vec{a} \cdot \vec{b} = ?$
5. $\vec{a} = 2\hat{i} + \hat{j} + 3\hat{k}$ and $\vec{b} = 3\hat{i} + 5\hat{j} - 2\hat{k}$ find (i) $\vec{a} \times \vec{b} = ?$ (ii) $|\vec{a} \times \vec{b}| = ?$
6. The angle b/w the vector $2\hat{i} + 3\hat{j} + 2\hat{k}$ and $\hat{i} - 4\hat{j} + 5\hat{k}$ is
7. If $\vec{a} = 2\hat{i} - 3\hat{j} - 5\hat{k}$ and $\vec{b} = -7\hat{i} + 6\hat{j} + 8\hat{k}$ find (i) $\vec{a} \cdot \vec{b}$ (ii) $\vec{a} \times \vec{b}$
8. $|\vec{a}| = \sqrt{26}$ $|\vec{b}| = 7$ and $|\vec{a} \times \vec{b}| = 35$ find $\vec{a} \cdot \vec{b} = ?$
9. Prove that $(\vec{a} - \vec{b}) \times (\vec{a} + \vec{b}) = 2(\vec{a} \times \vec{b})$
10. The projection of $4\hat{i} + 4\hat{j} - 6\hat{k}$ on $4\hat{i} - 7\hat{j} + 4\hat{k}$ is
11. If $6\hat{i} + 3\hat{j}$, $40\hat{i} - 8\hat{j}$, $x\hat{i} - 52\hat{j}$ are colinear find x.
12. $x\hat{i} + 2\hat{j} + z\hat{k} = 2\hat{i} + y\hat{j} + \hat{k}$ find x, y, z
13. Evaluate $(3\vec{a} - 5\vec{b}) \cdot (2\vec{a} + 7\vec{b})$
14. If a is unit vector then $(\vec{x} - \vec{a})(\vec{x} + \vec{a}) = 8$ find $|\vec{x}| = ?$
15. Find length of projection of $\vec{a} = \hat{i} + a\hat{j} + \hat{k}$ at $\vec{b} = 4\hat{i} - 4\hat{j} + 7\hat{k}$
16. If $|\vec{a} \times \vec{b}| = |\vec{a} \cdot \vec{b}|$ then find angle b/w \vec{a} and \vec{b} .
17. Prove that the point $2\hat{i} + \hat{j} + \hat{k}$, $6\hat{i} - \hat{j} + 2\hat{k}$ and $14\hat{i} - 5\hat{j} + 4\hat{k}$ are collinear
18. If $3\hat{i} - 2\hat{j} + 9\hat{k}$ and $\hat{i} - 2p\hat{j} + 3\hat{k}$ are parallel then p = ?
19. If $\vec{a} = 2\hat{i} - 4\hat{j} - 5\hat{k}$ and $\vec{b} = 2\hat{i} + 2\hat{j} + 4\hat{k}$ find (i) Area of ΔABC
(ii) Area of parallelogram
20. Prove that $(\vec{a} \times \vec{b})^2 + (\vec{a} \cdot \vec{b})^2 = a^2 - b^2$
21. If $\vec{a} + \vec{b} + \vec{c} = 0$ then prove that $\vec{a} \times \vec{b} = \vec{b} \times \vec{c} = \vec{c} \times \vec{a}$
22. If $\vec{a} = \hat{i} + 2\hat{j} + 3\hat{k}$, $\vec{b} = 3\hat{i} + 2\hat{j} + \hat{k}$ then $\cos \theta = ?$
23. Show that point $4\hat{i} + 5\hat{j} + \hat{k}$, $\hat{j} - \hat{k}$, $3\hat{i} + 9\hat{j} + 4\hat{k}$ and $-4\hat{i} + 4\hat{j} + 4\hat{k}$ are coplanar
24. If $3\hat{i} - 2\hat{j} + 9\hat{k}$ are $\hat{i} - 2\hat{j} + 3\hat{k}$ are collinear find p = ?
25. $\vec{a} = \hat{i} + \hat{j} + 2\hat{k}$, $\vec{b} = 3\hat{i} + 2\hat{j} - \hat{k}$ find $(\vec{a} + 3\vec{b}) \cdot (2\vec{a} - \vec{b}) = ?$

► **RELATION AND FUNCTION**

1. A = {1, 2, 3} and R = { (2, 2), (3, 3), (2, 3), (3, 2), (2, 1)} What types of Relation.

2. Show that the relation R in the Set $A = \{1, 2, 3, 4, 5\}$ given by $R = \{(a, b) : |a - b| \text{ is even}\}$ is an equivalence Relation
 3. $R = \{(a, b) : a, b \in \mathbb{Z} \text{ and } a - b \text{ is divisible by } 5\}$ is an equivalence R.
 4. $A = \{1, 2, 3\}$ $R = \{(1, 1), (2, 2), (3, 3), (1, 2), (2, 1), (2, 3), (3, 2), (1, 3), (3, 1)\}$

Prove that

▶ FUNCTION BINARY COPERATION INVERSE

1. F : N → N be a fⁿ defined as f(x) = 9x + 3 show that f is one-one fⁿ.
 2. F : R → R and f(x) = 2x show that it is on to fⁿ.
 3. F : R → R be a fⁿ defined as by f(x) = 4x³ – 7 show that It is bijective fⁿ.
 4. f(x) = 3x – 4 and f(x) = 10x + 7 is define F : R → R then find F⁻¹(x)
 5. F : R → R such that f(x) = 4x + 3 find f⁻¹(x)
 6. F : R → R such that f(x) = 2x + 3 find f⁻¹(x)
 7. If a * b = a² – b² then (1 * 2) * 6 = ?
 8. If x * y = 1 + 12x + xy \forall x, y \in θ find (2 * 3)
 9. f(x) = 8x³ and g(x) = x^{1/3} find gof
 10. If f(x) = $\frac{x+3}{2}$ and g(x) = 2x – 3 find fog and gof
 11. If f(x) = $\frac{3x+4}{5x-7}$ find gof(x) and fog(x)
 12. f(x) = (3 – x³)^{1/3} find fo f
 13. * defined on N such that a * b = LCM 20 * 16 then show that * is commutative.

► INCREASING & DECREASING

1. Discuss increasing and decreasing Natur of $f(x) = 2x^3 - 15x^2 + 36x + 4$
 2. Discuss increasing and decreasing natur of $f(x) = 4 x^3 - 6 x^2 - 72 x + 30$

► MAXIMA AND MINIMA

- Find Maximum and minimum value of $f(x) = 2x^3 - 15x^2 + 36x + 1$ on the $[1, 5]$
Ans :- (56, 24)
 - $f(x) = 12x^{4/3} - 6x^{1/3}$, $x \in [-1, 1]$ Ans :- 18, -9/4
 - Find two numbers whose sum is 24 abd whose product is large possible.
 - Find two positive number x & y such that $x + y = 60$ and xy^3 is maximum

➤ **ROLLES THEOREM**

1. If $f(x) = x^2 + 4$ in $[-1, 1]$ then find C by Rolles theorem
2. Verify Rolles theorem for the function $f(x) = 2x^3 + x^2 - 4x + 2$ in $\left[-\frac{1}{2}, \sqrt{2}\right]$
3. Verify Rolles theorem $f(x) = \sin x + \cos x$ in $[0, \frac{\pi}{2}]$

➤ **MEAN VALUE THEOREM M.U.T.**

1. Verify M.U.T if $f(x) = (x - 1)(x - 2)(x - 3)$ in $[0, 4]$
2. Find the value of C By M.U.T.
 - (a) $F(x) = 2x^2 - 10x + 29$ in $[2, 7]$
 - (b) $f(x) = x^3 - 3x^2 + 2x$ in $\left[0, \frac{1}{2}\right]$

➤ **TANGENT AND NORMAL**

1. Find the slope o tangent to the curve $y = x^3 - x$ at $x = 2$
2. Find the slope of tangent to the curve $y = x^3 + x + 1$ at x – co-ordinate is 2.
3. Find the slope of the Normal to the curve $y = 2x^2 + 3 \sin x$ at $x = 0$ is
4. Find the point at which the tangent to the curve $y = \sqrt{4x - 3} - 1$ has Its slope $2/3$.
5. Find the slope of normal at point $(1, 1)$ of the curve. $y = x^2 + 3x - 4$

➤ **APPROXIMATION**

1. Find Approximate value sing differentiation if
 - (a) $\sqrt{36.6}$
 - (b) $\sqrt{49.5}$
 - (c) $(401)^{\frac{1}{2}}$
 - (d) $\left(\frac{17}{81}\right)^{\frac{1}{4}}$
2. Find the approximate value of $f(3.02)$ where $f(x) = 3x^2 + 5x + 3$
3. the approximate change n the volme of a cube of side x m cubed by increasing the side by 3% is

➤ **RATE OF CHANGE OF QUANTITIES**

1. Find the rate of change of the area of a circle with respect to Its r. when (i) $r = 5$ cm (ii) $r = 3$ cm
2. The radius of 21 circle is increasing at the rate of 0.7 cm/s What is the rate of increasing of Its circumference.
3. A balloon which always remains spherical has a variable radius. Find the rate at which its volume is increasing with the radius when the later is 10 cm.

➤ **DIFFERENTIAL EQUATION**

Find order and degree

1. $\left(\frac{d^2y}{dx^2}\right)^2 + 2\left(\frac{dy}{dx}\right)^3 + 9y = \sin x$
2. $y^{111} + 2y^{11} + y^1 = 0$
3. $\left(\frac{d^2y}{dx^2}\right)^2 + \cos\left\{\frac{dy}{dx}\right\} = 0$
4. $8x^2 \frac{d^2y}{dx^2} + 7\left(\frac{dy}{dx}\right)^2 + 9 = 0$
5. $(y^{111})^2 + (y^{11})^3 + (y^1) + y^5 = 0$
6. Solve $x \frac{dy}{dx} - y = 2x^2$
7. Solve $(\tan^{-1}y - x) \frac{dy}{dx} = (1 + y^2)dx$
8. solve $(x^3 + y^3)dy - x^2ydx = 0$
9. $\frac{dy}{dx} + y \cdot \cot x = 2x + x^2 \cot x$
10. Solve $\frac{dy}{dx} = e^{x+y}$
11. $\frac{dy}{dx} + \frac{y}{x} = \frac{y^2}{x^2}$
12. $\frac{dy}{dx} = \frac{x}{y}$ solve
13. Solve $\frac{dy}{dx} - \frac{2y}{x} = y^4$
14. Solve $y dx - (x + 2y^2) dy = 0$
15. Solve $(x - y)dy - (x + y)dx = 0$

➤ **B * AREA BOUNDED BY CURUE ***

1. Find the area bounded by parabola $y^2 = x$ and the line $x + y = 2$ above the x-axis
2. Find the area of smaller part of the circle $x^2 + y^2 = a^2$ by the line $x = a/2$
3. Find the area bounded by curve $x^2 = 4y$ and line $x = 4y - 2$
4. Find the area of the circle $4x^2 + 4y^2 = 9$ which is interior to the parabola $x^2 = 4y$
5. Find the area of the region bounded by the ellipse $\frac{x^2}{16} + \frac{y^2}{9} = 1$

➤ **C * CONTINUITY AND DIFFERENTIABILITY ***

1. Is $f(x) = \begin{cases} x^3 - 3, & x \leq 2 \\ k, & x > 2 \end{cases}$ continuous at $x = 2$ Find the value of k .
2. Find the value of 'a' and 'b' such that the f^n defined by $f(x) = \begin{cases} 5 & \text{if } x \leq 2 \\ ax + b & \text{if } 2 < x < 10 \\ 21 & \text{if } x \geq 10 \end{cases}$ is continuous
3. $f(x) = \begin{cases} x^2 + 3x + a & \text{when } x \leq 1 \\ bx + 2 & \text{when } x > 1 \end{cases}$ is differentiable find a & b

➤ **PROBABILITY**

1. If A and B are two events such that $P(A) = \frac{1}{3}$, $P(B) = \frac{1}{7}$ and $P(A \cap B) = \frac{1}{5}$ then $P\left(\frac{A}{B}\right)$ and $P\left(\frac{B}{A}\right)$

2. $P(A) = \frac{3}{8}$ $P(B) = \frac{5}{8}$ $P(A \cup B) = \frac{3}{4}$ then $P\left(\frac{B}{A}\right) = ?$
3. $P(A) = \frac{3}{8}$ $P(B) = \frac{1}{3}$ $P(A \cap B) = \frac{1}{4}$ find $P(\bar{A} \cap \bar{B}) = ?$
4. $P(A) = \frac{3}{8}$ $P(B) = \frac{1}{2}$ $P(A \cap B) = \frac{1}{4}$ find $P(\bar{A}/\bar{B}) = ?$
5. $P(A \cup B) = \frac{3}{4}$, $P(A \cap B) = \frac{1}{4}$ and $P(\bar{A}) = \frac{2}{3}$ find $P(\bar{A} \cap B) = ?$
6. If A and B are two events such that $P(A) = \frac{1}{4}$ $P(B) = \frac{1}{3}$ and $P(A \cup B) = \frac{1}{2}$ then prove that A and B are independent event
7. A pair of dice is rolled. Find the probability of obtaining an even prime on each dice.
8. A speaksibe truth is 75% cases and B is 50% of the cases. In What percentage of case are they lively to contraidict each in statily the same fact.
9. Find :-
- | | | | | | | | | | |
|------|---|----|----|----|----|-----|-----|-----|-----|
| X | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| P(X) | a | 3a | 5a | 7a | 9a | 11a | 13a | 15a | 17a |
- (i) $P(x \leq 3)$ (ii) $P(x \geq 5)$ (iii) $P(2 \leq x \leq 7)$ (iv) $a = ?$

10. Find

X	0	1	2	3	4	5	6	7
P(X)	0	K	$2k$	$2k$	$3k$	k^2	$2k^2$	$7k^2 + k$

(i) k (ii) $P(x < 6)$ (iii) $P(x \geq 2)$

11. $P(A) = \frac{1}{2}$ $P(B) = 0$ then $P\left(\frac{A}{B}\right)$ is
12. If $P\left(\frac{A}{B}\right) = P\left(\frac{B}{A}\right)$ then
13. $P(A) = \frac{1}{2}$ $P(A \cap B) = \frac{3}{5}$, $P(B) = P$ find P
 (i) Mutualy excusive (ii) independent
14. In a box containing 100 bulbs, 10 are defective the probability of out of a sample of 5 bubs, none is defective.

➤ **3-d & PLANE**

- Find the direction cosine of x-axis, y-axis and z-axis.
- $l^2 + m^2 + n^2 = ?$ Or, $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = ?$ Or $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma = ?$
- Find the shortest distance b/w lines

$$\frac{x-3}{2} = \frac{y-4}{1} = \frac{x+1}{3} \text{ and } \frac{x-1}{-1} = \frac{y-3}{3} = \frac{z-1}{2}$$

4. The direction ratio of normal to the plane $7x + 4y - 2z + 5 = 0$ are
 5. The direction cosine of noral to the plane $2x - 3y - 6z - 3 = 0$ are
 6. Find the distance of plane $2x - 3y + 6z + 7 = 0$ from the point $(2, -3, -1)$
 7. Find the eqⁿ of the line passing through $(2, -1, 3)$ and direction ratio $(3, -1, 2)$
 8. Find the direction ratio of the line (x_1, y_1, z_1) and (x_2, y_2, z_2)
 9. If the lines $\frac{x-1}{-3} = \frac{y-2}{2k} = \frac{z-3}{2}$ and $\frac{x-1}{3k} = \frac{y-1}{1} = \frac{z-6}{-5}$ are perpendicular find the value of k.
 10. Find the eqⁿ of the plane parallel to $2x + 5y - 6z + 3 = 0$ and passes $(1, 1, 1)$
 11. Find the eqⁿ of the plane passing through the point $(0, 7, -7)$.
 12. The cartesian eqⁿ of the line is $\frac{x+2}{2} = \frac{y-5}{4} = \frac{z+6}{2}$
 13. Show that $\frac{x-5}{7} = \frac{y+2}{-5} = \frac{z}{1}$ and $\frac{x}{1} = \frac{-y}{2} = \frac{z}{3}$ are \perp each other
 14. Find the vector and cortesian eqⁿ of the line that passes through the point $(3, -2, -5)$ & $(3, -2, 6)$
 15. Find the value of P so that the line $\frac{1-x}{3} = \frac{7y-14}{2P} = \frac{z-3}{2}$ and $\frac{7-7x}{3P} = \frac{y-5}{1} = \frac{6-z}{5}$ are right angle

➤ **MIXED PROBLEM**

1. $y = \cos(\log x)$ then $\frac{dy}{dx} = ?$

2. (i) $\vec{a} \times \vec{b} = ?$ (ii) $\hat{i} \times \hat{j} = ?$

(ii) $\vec{a} \perp \vec{b}$ then $\vec{a} \cdot \vec{b} = ?$ (iv) $\hat{k} \cdot \hat{k} = ?$

3. The I.F of diff. equation $\frac{dy}{dx} + Py = q$ is

4. the order and degree of diff. eqⁿ $\left(\frac{d^2y}{dx^2}\right)^2 - x \left(\frac{dy}{dx}\right)^3 = y^3$ is

5. $\tan^{-1}(\sqrt{3}) - \cot^{-1}(-\sqrt{3})$

6. Prove that $\tan^{-1}x + \tan^{-1}\left(\frac{2x}{1-x^2}\right) = \tan^{-1}\left\{\frac{3x-x^3}{1-3x^2}\right\}$

7. $\cos[\tan^{-1}\{\sin(\cos^{-1}x)\}] = \sqrt{\frac{1+x^2}{2+x^2}}$

8. Show that $\tan\left\{\frac{1}{2} \sin^{-1}\frac{3}{4}\right\} = \frac{4-\sqrt{7}}{3}$

9. $\int \frac{x \cdot \sin^{-1} x}{1-x^2} dx$
10. Write the vector eqⁿ line $\frac{x-5}{3} = \frac{y+7}{7} = \frac{6-z}{2}$
11. $l^2 + m^2 + n^2 = ?$
12. $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma = ?$
13. $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = ?$
14. Find the value of λ lines are \perp each other $\frac{x-5}{3\lambda+2} = \frac{2-y}{5} = \frac{1-z}{-1}$ and $\frac{x}{1} = \frac{2y+1}{4\lambda} = \frac{1-z}{-3}$
15. $f(x) = x^2 + 4$ find $f^{-1}(x)$
16. If $y = e^x \{ \sin x + \cos x \}$ then prove that $\frac{d^2y}{dx^2} - 2 \frac{dy}{dx} + 2y = 0$
17. $F : R \rightarrow R$ be a fⁿ and $f(x) = 4x^3 + 7$ is bijective fⁿ.
18. $h(A) = 2$ $n(B) = 2$ then $n(A \times B) = ?$
19. $F : N \rightarrow N$ as $f(n) = \begin{cases} \frac{n+1}{2} & \text{when } n \text{ is odd} \\ \frac{n}{2} & \text{when } n \text{ is even} \end{cases}$ $\forall x(n)$ show that bijective
20. Prove that $\begin{vmatrix} a & b & c \\ a-b & b-c & c-a \\ b+c & c+a & a+b \end{vmatrix} = a^3 + b^3 + c^3 - 3abc$